Accounting for Work Life Expectancy: Applying the Skoog-Ciecka-Krueger Transition Probabilities

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<u>Abstract</u>

While many forensic economists rely on the Skoog-Ciecka-Krueger work life tables, few seem to make use of the labor force transition probabilities provided as supplemental material to the published tables. This paper explains the calculations needed to compute the probability of labor force activity for a person who is an initially active or an initially inactive labor force participant based on these transition probabilities. Following this explanation, the explicit use of the probability of labor force activity is compared to the common methods of accounting for work life expectancy. The paper concludes by identifying the issues that use of the probability of labor force activity presents.

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I Introduction

Many forensic economists recognize that future lost earnings will not be attained with certainty and consequently reduce their loss estimates to account for the risk of death, injury, sickness and other events that would keep an individual from being an active labor force participant. For example, in the *2012 Survey of Forensic Economists* (Slesnick, Luthy and Brookshire, 2013), only 7.8 percent of the respondents indicated they ended their loss calculation at some fixed retirement date; 3.0 percent used the LPE method; and 70.3 percent of the remaining respondents indicated they relied on work life tables published in economic journals. The latest such tables, and perhaps the most widely used, are those found in Skoog, Ciecka, and Krueger (2011) – hereinafter "S-C-K". Less widely used are the labor force transition probabilities that were provided as supplemental materials to the S-C-K work life tables.

This paper presents the calculations required to compute the probability of labor force activity for persons of a given age, gender, level of educational attainment and initial labor force status using the S-C-K transition probabilities and extended versions of published life tables. Following this explanation, the explicit use of the probability of labor force activity is compared to the common methods of accounting for work life expectancy (WLE). The paper concludes by identifying the issues that use of the probability of labor force activity presents.

II <u>Required Calculations</u>

Calculating the probability of being an active labor force participant is most easily understood in the context of modeling the size of a synthetic cohort of initially active individuals as the cohort ages, while at the same time calculating the number of deaths and the number of living inactive individuals. (For the

corresponding probability of an initially inactive person, the modeled cohort corresponds to initially inactive persons; the number of active persons and the number of deaths are also calculated.) This approach is similar to the calculations underlying a period life table, in which the number of deaths and remaining living persons from an initial cohort is calculated as the cohort ages. A specific example will illustrate the calculation of the probability of being an active labor force participant.

Starting with 100,000 living females at age 30, the number of actives (A_{30}) is set equal to 100,000, and the number of living inactive (IA_{30}) and deaths (D_{30}) are both set equal to zero. At age 31, these values are recalculated as follows:

- (1) $A_{31} = A_{30} \cdot {}^{a}\rho {}^{a}{}_{30} + IA_{30} \cdot {}^{i}\rho {}^{a}{}_{30};$
- (2) $IA_{31} = A_{30} \cdot {}^{a}\rho {}^{i}{}_{30} + IA_{30} \cdot {}^{i}\rho {}^{i}{}_{30}$; and
- (3) $D_{31} = (A_{30} + IA_{30}) \cdot (1 l_{31}/l_{30}),$

where ${}^{a}\rho_{x}^{a}$ is the probability of someone who is age x transitioning from the active to the active state; ${}^{i}\rho_{x}^{i}$ is the probability of transitioning from the inactive to the inactive to the active state; ${}^{i}\rho_{x}^{i}$ is the probability of transitioning from the inactive to the inactive state; ${}^{a}\rho_{x}^{i}$ is the probability of transitioning from the active to the inactive state; ${}^{a}\rho_{x}^{i}$ is the probability of transitioning from the active to the inactive state; and where l_{x} is the number of living persons age x taken from the life table. The ${}^{a}\rho_{x}^{a}$, ${}^{i}\rho_{x}^{i}$, and ${}^{a}\rho_{x}^{i}$ incorporate the probability of survival; that is, they are the S-C-K transition probabilities multiplied by one minus the probability of death. Note that one minus l_{x}/l_{x-1} equals the probability of death.

At age 32, the values are recalculated again, as follows:

- (1) $A_{32} = A_{31} \cdot {}^{a} \rho^{a}_{31} + I A_{31} \cdot {}^{i} \rho^{a}_{31};$
- (2) $IA_{32} = A_{31} \cdot {}^{a}\rho {}^{i}_{31} + IA_{31} \cdot {}^{i}\rho {}^{i}_{31}$; and
- (3) $D_{32} = (A_{31} + IA_{31}) \cdot (1 \ell_{32}/\ell_{31}).$

These calculations are repeated for all subsequent ages through some terminal age after which no remaining cohort members are active. The probability of being an active labor force participant at age x, P_x , is calculated as A_x divided by the initial size of the synthetic cohort (100,000). While it is not

necessary to calculate the number of deaths in step (3), doing so allows one to check the calculations in steps (1) and (2) since $D_{x+1} = \int_x -A_{x+1} - IA_{x+1}$ for all ages.

The required calculations are similar when the initial labor force status is inactive: the number of living inactives (IA₃₀) is set equal to 100,000, and the number of actives (A₃₀) and deaths (D₃₀) are both set equal to zero. At age 31, and for all subsequent ages through the terminal age, these values are recalculated as outlined above. The probability of being an active labor force participant at age x is still calculated as A_x divided by the initial size of the synthetic cohort. This calculation is equivalent to one minus the sum of IA_x and the total cumulative deaths divided by the initial size of the synthetic cohort. Note that this sum is the total number of inactive persons – both living and deceased – out of the initial cohort at age x.

Figure 1 presents the calculation of the probability of labor force activity for an initially active 30-year old female with an Associate's degree in spreadsheet form. Figure 2 presents the corresponding calculations for the initially inactive state. In both figures, columns B through E contain the S-C-K transition probabilities for a female with an Associate's degree from age 30 on; these probabilities are <u>not</u> conditioned on the probability of survival. Column F contains the values of the l_x from the 2006 life tables for females.¹ These values are used to calculate the number of survivors at each successive age in column G, given the starting cohort value of 100,000. The number of survivors at age x+1 equals the survivors at age x times the ratio of l_{x+1} to l_x . This ratio equals the probability of a person age x living to age x+1.

The number of cohort members who are active (and alive) is calculated in column H. It equals the number of active cohort members from the prior age times the probability of transitioning from the active to active state, plus the number of living inactive cohort members from the prior age times the probability of transitioning from the living inactive to the active state. This sum is multiplied by the probability of surviving one year from the prior age in order to account for the active and living inactive cohort members who will die within that year.

The number of cohort members who are alive and inactive is calculated in column I. It equals the number of active cohort members from the prior age times the probability of transitioning from the active to inactive state, plus the number of living inactive cohort members from the prior age times the probability of transitioning from the living inactive to the living inactive state. Again, this sum is multiplied by the probability of surviving one year from the prior age in order to account for the active and living inactive cohort members who will die within that year.

Column J calculates the number of cohort members who have died at each age: it equals the number living at the prior age times one minus the probability of surviving one additional year. As noted earlier, the number of deaths is not needed to calculate the probability of being active in the labor force; it is used to check the validity of the other calculations. This is done in column K which equals the number living for the prior age in column G minus the number of alive and active, the number of alive and inactive, and the number of deaths in columns H, I and J.

The probability of being active is calculated in column L: it equals A_x divided by the initial cohort size of 100,000. The sum of column L equals the mean WLE. Because all of the foregoing calculations assume end-of-year transitions, for initially active persons the resulting sum is 0.5 years higher than those reported in the published S-C-K tables. Consequently, the mid-year adjustment shown at the bottom of Figure 1 is needed to tie to the published WLE values. No such adjustment is needed in Figure 2 for initially active persons. The reason for this is that the sum of column L is really sum of each probability times the period of time each probability corresponds to. For end-of-year transitions, this period is one year for all terms in the sum, while for mid-year transitions it is 0.5 years for the first term of the sum, and one year for all others. The difference between end-of-year and mid-year transitions consequently equals the difference between the two first terms of these summed products. For initially active persons, this difference equals (100% x 1) minus (100% x 0.5), which equals 0.5 and gives rise to the mid-year adjustment shown at the bottom of Figure 1. For initially inactive persons, this difference equals (0% x 1) minus (0% x 0.5), which equals zero and obviates the need for the mid-year adjustment.

An alternative to the mid-year adjustment is shown in column M, which calculates the average of P_x and P_{x+1} for each age x. This column is an estimate of the probability of labor force activity at mid-year. Consequently, the sum of the average probabilities in column M equals the WLE based on mid-year transitions and requires no further adjustment. These average probabilities are also consistent with mid-year discounting of annual losses.

The calculations outlined above produce the probability of being active for a female who is exactly 30 years old. It would be an extreme coincidence if the date of the injury, death or other triggering event corresponded exactly to a plaintiff's or decedent's birthday. More often than not, the probability of being active is needed for a person who is not exactly an integer number of years old. The solution to this problem is relatively straightforward and is similar to that explained by Tucek (2009) in connection with the survival probability of a person with a non-integer age. Suppose, for example, we were dealing with a female who was 30.4 years old instead of exactly 30 years old. The desired probability of being active may be calculated by first calculating the number of living and active persons (A_x) for a 30-year old starting with an initial cohort of 100,000 at age 30, along with the number of living and active persons (\tilde{A}_x) for a 31-year old starting with an initial cohort of 100,000 at age 31. The weighted average of A_x and \tilde{A}_{x+1} , with the weights being determined by the fractional part of the individual's age, can be used to calculate the probability of being an active labor force participant. Note that the larger weight is assigned to the set of living and active cohort members closer to the individual's age. In our example, A_x would be assigned a weight of 0.6, while \tilde{A}_x would be assigned a weight of 0.4.²

III <u>Comparison with Common Methods of Accounting for WLE</u>

Skoog and Ciecka (2006) identified two principle approaches adopted by forensic economists when dealing with WLE. They either assume the WLE comes immediately (front loading) or they spread the WLE over a larger number of years, say to the full Social Security retirement age (uniform loading). Compared to calculating the expected present value of a constant annual loss based on the years of labor force activity at each future age, Skoog and Ciecka showed that front loading overstates the estimated loss

for a variety of (positive) net discount rates. Similarly, they showed that uniform loading sometimes overstates and sometimes understates the expected present value of the lost earnings. A variation of front loading is to present the loss estimates with certainty for several years beyond WLE, ostensibly to give the jury the latitude to decide whether the plaintiff would have been an active labor force participant for fewer or more years than WLE suggests. This is characterized as the "WLE plus N" variant of front loading in the discussion below.

All of these approaches are shortcuts in the sense that they replace the probability of labor force activity at each future age with an easily calculated alternative. Front loading sets the probability of labor force activity equal to one up to the age that WLE is reached, and to zero thereafter. The "WLE plus N" variant does the same thing, for an additional N years. Uniform loading sets the probability to some fraction, f, equal to WLE divided by the number of years until some specified age is reached for ages less than or equal to that specified age, and to zero thereafter. In Figure 3 these alternatives are compared to the probability of labor force activity for an initially active 30-year old female with an Associate's degree calculated using the S-C-K transition probabilities and the (extended) 2006 life table for females. In this example, the alternative uniform loading probability is based on spreading the 29.61 years of work life through age 67 and equals 0.8003 (29.61 divided by 37).

One of the major shortcomings of these alternatives is illustrated in Figure 4, which depicts a familiar age-earnings profile for a female with an associate's degree. In this figure, the actual data points corresponding to each age step are depicted by the X's. The profile is created by a linear spline connecting the midpoints of each step.³ Unless the ending age assumed for uniform loading extends beyond the late sixties, both front and uniform loading of WLE force all of the plaintiff's or decedent's remaining WLE into the years when earnings are expected to be highest. In other words, both methods ignore the typical decline in earnings after some point, even though the probability of continued labor force activity is greater than zero well beyond the age at which the WLE would have been exhausted

under either method. Even though both front and uniform loading result in the same estimate of WLE, in terms of the present value of the expected loss, they both have an *a priori* upward bias.

A second major shortcoming of both these methods stems from the implicit assumption that, if the plaintiff or decedent worked full time prior to the event leading to the tort, then they will always work full time. This is a reasonable assumption for most individuals only up to a point. Even though there is a nonzero probability of labor force activity at age 70, 75 or even age 80, it may not be reasonable to assume that it will involve full-time employment. If it is not, then both front and uniform loading will consequently overstate the expected earnings loss because they truncate the loss at too early of an age.⁴

Finally, the front-loading variant of "WLE plus N" introduces its own, unique, shortcoming by transforming the decision to be made by the jury. The jury no longer has to decide on a reasonable estimate of the plaintiff's expected earnings loss that is informed by the probability that the plaintiff would remain in the labor force, but must now make a decision on the basis of a small number of loss estimates computed with certainty for a range of ages around the age at which the plaintiff's WLE is reached. All of the estimates from this age and beyond will necessarily overestimate the expected loss, as may the estimates just before this age. This is illustrated in Figure 5. This figure portrays the probability mass function for a 30-year-old woman with an associate's degree - it is a picture of how the possible work life outcomes are distributed.⁵ In this figure, the age at which WLE is reached is 59.6 years, and the range defined by plus or minus one standard deviation (51.7 to 67.5 years) encompasses 71 percent of such outcomes. It is not reasonable to expect a jury to do anything more than select the midpoint of such a wide interval, so setting "N" equal to 7.9 years provides no more useful information concerning the expected loss than does front loading. Setting "N" to a smaller number, say, three years, still provides no useful information concerning the expected loss and ignores the effect of the non-zero probabilities beyond the age at which WLE is reached. In short, the "WLE plus N" variant is really just front loading in disguise. Even if earnings do not decline beyond some age, losses computed with certainty for age

59.6 and beyond will overstate the expected loss, as will estimates computed with certainty for a few years earlier.

IV Discussion

It is clear from Figure 3 that non-zero probabilities of labor force activity extend well beyond the age WLE is reached. The reason for this is not that the S-C-K transition probabilities and the probability of survival extend to age 110, the terminal age in the underlying Markov increment/decrement model.⁶ The reason is that some individuals actively participate in the labor force at ages well beyond WLE and beyond what is loosely referred to as a normal retirement age. Because they do not account for this, shortcut methods like front loading and uniform loading are only approximations to the impact of the risks preventing someone from participating in the labor force. How close the approximations are depends on the expected years of labor force activity beyond the age WLE is reached for front loading, and on the expected years of labor force activity beyond the presumed permanent labor force exit for uniform loading. In terms of present value, it also depends on how far in the future the age that WLE is reached, and on the interest rate used to discount future losses to the present. Because the presumed age of permanent labor force exit is typically greater than the age at which WLE is reached, uniform loading will be the better of the two shortcut approximations, other things being equal. In practice, none of the shortcut methods account for the effect of part-time employment at advanced ages and are biased upwards for this reason as well.

If the possible work life outcomes were tightly distributed about their mean, neither the "WLE plus N" variant nor simple front loading would misstate the expected loss to a great extent. And, if this were the case, expectations of the age at which an earnings loss ends would be close to the age at which WLE is reached, making uniform loading nearly the same as front loading. Unfortunately this is not the case: all of the work life outcomes corresponding to the published tables are widely distributed about their means. For active males, the coefficient of variation (the standard deviation divided by mean WLE) ranges from a low of 22 to a high of 97 percent. For active females, the range is 22 to 92 percent. For inactive males

and females the ranges are 23 to 359 percent and 23 to 486 percent. Although the variation in the distribution of work life outcomes increases in relative terms for both males and females as age increases, it decreases in absolute terms. However, the standard error falls below 3 years only at very late ages – no earlier than age 62 for males (initially inactive with no diploma or GED) and 58 for females (initially inactive with no diploma or GED) and 58 for females (initially inactive with no diploma or GED). Thus, the instances in which arbitrarily setting "N" to a low number might result in a range of at least plus or minus <u>one</u> standard deviation are limited to older plaintiffs and decedents.

Compared to any of the shortcut methods, explicit calculation of the probability of labor force activity offers several advantages. First, and most important, there is no *a priori* bias in the resulting estimate of the expected loss because it estimates the expected loss directly and accounts for the wide variation in work life outcomes. Second, explicit calculation of the probability of labor force activity allows one to use updated mortality tables and to account for the implicit assumption that an injured plaintiff will be alive on the date of the trial.

A third advantage arises in cases where a loss is contingent upon the survival of a plaintiff who is not the injured person or decedent – financial support or medical insurance provided to a spouse are examples. The expected present value of such losses necessarily depends on the survival probability of the non-injured plaintiff. And, if the loss is also contingent on the employment of the injured person, explicit use of the probability of labor force activity in lieu of front or uniform loading provides a consistent means of accounting for the risk that the loss component may not have been realized even if the event leading to the tort had not occurred.⁷

Finally, explicit calculation of the probability of labor force activity allows consideration of part-time employment at older ages and does not force all of the labor force activity into earlier, higher income years. Nevertheless, there are drawbacks to using the probability of labor force activity in lieu of any of the three shortcut methods. For one thing, the required calculations are necessarily more complex. Additionally, using the full range of the probability of labor force activity requires an estimate of earnings for years beyond age 70.

Even though the calculations are more complex than those required by any of the shortcut methods, they are within the reach of any competent forensic economist and can easily be performed using an Excel spreadsheet or other application. More important, just because the calculations are complex doesn't mean that the explanation has to be. To object to use of the probability of labor force activity because of complexity is to abdicate one's role as an expert: if use of only simple calculations were a requirement for loss estimates, then the courts would have little need for economic experts. It is clearly not necessary to explain how the probability of labor force activity is calculated, just as it is not necessary to explain how present values or survival probabilities are calculated. It is sufficient only to explain that the underlying calculations take into account that the plaintiff may die, may become injured or sick, or may not be an active labor force participant for any other reason. In short, the same explanation as is given for WLE will suffice.

The need to estimate annual earnings for years beyond age 70 is a more substantive drawback. While use of an age-earnings profile may capture an expected decline in full-time earnings at older ages, it will not necessarily reflect the decrease due to part-time employment.⁸ The real issue, however, is whether assuming, as the alternative approaches do, that earnings equal zero once a certain age is reached is more reasonable than presenting earnings assumptions that cover the full range of the probability of labor force activity. It is possible to make reasonable assumptions about earnings beyond WLE or some assumed retirement age, and to present the loss estimates in such a way that the jurors can adjust them as they believe best, based on the specifics of the case. Table 1 presents an example of how this may be done. In this example, it is assumed that part-time employment at half the full-time earnings starts at age 70. If the jurors believe that the part-time earnings would be only one-fourth the full-time level, it is easy to explain

that they need only subtract half of the \$30,000 from the total to arrive at a total loss of \$315,000. Similarly, if they believe earnings will always be at the full-time level, it is easy to explain that they need only add \$30,000 to the total.

V Conclusions

This paper has presented the calculations needed to compute the probability of labor force activity for a person who is an initially active or an initially inactive labor force participant using the S-C-K transition probabilities. Three alternatives to the explicit use of the probability of labor force activity to estimate an expected earnings loss were identified: (1) front loading; (2) uniform loading; and (3) the WLE plus N variant of front loading. As shown in Figure 3, each of these alternatives replaces the probability of labor force activity at each future age with an easily calculated substitute. These substitutes shift the probability of labor force activity to younger ages and set it to zero at some point even though the S-C-K transition probabilities produce greater-than-zero probabilities of labor force activity at ages beyond this point. This shifting creates an *a priori* bias in each of the shortcut alternatives by forcing all of the remaining labor force activity into the years when earnings can be expected to be highest and by ignoring a decline in earnings at later ages due to age-profile effects or to a shift to part-time employment. The wide variation in work life outcomes makes the shortcut alternatives less attractive than explicit reliance on the probability of labor force activity to estimate the expected earnings loss.

Explicit use of the probability of labor force activity offers several advantages: (1) it does not suffer from the *a priori* bias of the shortcut methods; (2) it allows one to use the most recent mortality tables and to explicitly account for the assumption that an injured plaintiff is alive on the date of the trial; (3) it permits consistent treatment of mortality risk when losses are incurred by non-injured plaintiffs; and (4) it does not ignore the decline in earnings due to age-profile effects or to a shift to part-time employment.

There are drawbacks to the explicit use of the probability of labor force activity: the approach is more complex and it requires earnings estimates at age 70 and beyond. The first drawback is easily overcome,

since the required calculations are within the reach of any competent forensic economist and since complex calculations do not necessitate complex explanations. The second drawback is more problematic, but can be overcome by presenting losses in the fashion illustrated in Table 1.

On balance, even though using the probability of labor force activity in lieu of other commonly-used alternatives requires a bit more explaining and a somewhat more detailed presentation of the loss estimates, the advantages seem to overcome the drawbacks. No one can say for certain what a plaintiff's future earnings would have been but for his injury. At best, a forensic economist can only estimate the expected loss. Because the alternative approaches move the loss earlier in time, and because earnings at ages beyond what is considered to be normal retirement may be lower, the alternatives have an *a priori* bias in favor of overstating the expected loss. At bottom, the fact that other means of accounting for WLE ignore the underlying probability distribution, as well as the possibility that earnings in the years beyond the age WLE is reached may very well be at a lower level, carries the decision in favor of fully utilizing the S-C-K transition probabilities as explained above.

References

- Arias, Elizabeth, "United States Life Tables, 2006", National Vital Statistics Report, 58(21), 2010, pp. 1-40, National Center for Health Statistics.
- Skoog, Gary R., James E. Ciecka and Kurt V. Krueger, "The Markov Process Model of Labor Force Activity: Extended Tables of Central Tendency, Shape, Percentile Points, and Bootstrap Standard Errors", *Journal of Forensic Economics*, 22(2), 2011, pp.165-229.
- _____, James E. Ciecka, "Allocation of Worklife Expectancy and the Analysis of Front and Uniform Loading with Nomograms", *Journal of Forensic Economics*, 19(3), 2006, pp. 261-296).
- Slesnick, Frank T., Michael R. Luthy, and Michael L. Brookshire, "A 2012 Survey of Forensic Economists: Their Methods, Estimates and Perspectives", *Journal of Forensic Economics*, 24(1), 2013, pp.67-99.
- Tucek, David G., "Calculating Survival Probabilities", *Journal of Legal Economics*, 2009, Vol. 16(1), pp. 111-126.

Calculating the Probability of Being An Active Labor Force Participant – Initially Active State

[A]	[B]	[C]	[D]	[E]	[F]	[G]	[H]	[1]	[J]	[K]	[L]	[M]
	S-C-K Tr	ansition Proba	bilities									
	Females Wit	th An Associate	's Degree	Tre	Traitic leading for small stip as heart					(1	00.00% + 93.78	%) ÷ 2
					Initial values for synthetic cohort.			100,000 ÷ 10	00,000			
		100,000 x 98,399 ÷ 98,461					100 A			Check		Average for
	Inactive to	Inactive to	Active to	Active to	4		Alive &	Alive &		Difference	Probability of	Discounting &
Age	Inactive	Active	Inactive	Active		Alive	Active	Inactive	Dead	On Alive	Being Active	Transitions
30	0.70303	0.29697	0.06164	0.93836	98,461	100,000	100,000	0	0	1	> 100.00%	¥ 96.89%
31	0.71164	0.28836	0.05738	0.94262	98,399	> 99,937	_ 93,776	6,160	63	0.00000	93.78%	, 91.94%
32	0.72864	0.27136	0.05540	0.94460	98,333	-> 99,870 /	90,111	9,759	67	7 0.00000	1 90.11%	1 88.91%
33	0.74605	00.027	00 222 - 00 20	4628	98,262	99,798	87,704	7 12,094	172	1 70.00000	87.70%	86.85%
34	0.75996	99,937	x 98,333 ÷ 98,35	4949	98,186	99,721	85,998 /	13,723 /	/ 77 /	0.00000	86.00%	85.44%
35	0.75831	(100.000 - (02926 + 0 - 0 2	0(07) - 08 3		99,638	84,878	14,761	83 /	0.00000	84.88%	84.53%
36	0.76535	(100,000 X ($0.93836 \pm 0 \ge 0.2$	9697) x 98,3	99 - 98,461	99,550	84,183	15,367 /	89/	/ 0.00000	84.18%	83.91%
37	0.76975	0.23025	0.04837	0.95163	97,923	99,453	\$3,632	1,8,827	96 j	0.00000	83.63%	83.39%
38	0.76201	(93,776 x 0.9	4262 + 6,160 x ().28836) x 98	,333 ÷ 98,399 🖌	99,348	83,141	/16,207	105 /	0.00000	83.14%	83.04%
39	0.76977	0.23023	0.04585	0.95415	97,705	99,232	82,942	/ 16/290	/ 116/	0.00000	82.94%	82.86%
40	0.76561	(0 = 0.7	10202 + 100 000	- 0.0(1(4) -	08 200 - 08 461	7 99,194	82,783	/ 1/6,321	/ 128	0.00000 /	82.78%	82.73%
41	0.75483	0 (0 X 0. /	10505 + 100,000	x 0.06164) x	98,399 - 98,461	98,963	82,681	/16,281	/ 141	0.00000 /	82.68%	82.67%
42	0.75451	0.24549	0.04638	0.95362	97,288	98,808	82,654	/ 16,155 /	1 55	0.00000 /	82.65%	82.65%
43	0.75211	(6.160 x 0.7	71164 + 93.776 x	0.05738) x 9	8.333 ÷ 98.399	98,639	82,645	/ 15,994/	/169	0.00000 /	82.64%	82.77%
44	0.75803	(0,200 12 01)				98,454	\$2,887 /	15,5¢6	/ 185	0.00000	(93.78% + 9	0.11%) ÷ 2
45	0.76781	0.23219	0.04227	0.95773	06 740	00 252	×83,062 ر	15,190	/ 202	0.00000	63.00%	02.9070
46	0.76876	0.23124	0.04105	0.95895	100,000 x (1 - 98	,399÷98,461)	_ 82,8 \$ 2	18,140	/ 220	0.0000¢	82.89%	82.84%
47	0.77808	0.22192	0.03999	0.96001	96 289	97.794	<u> </u>	/15,006 /	238	0.00090	82.79%	82.69%
48	0.79302	0.20698	0.04037	0.95963	99,937 x (1	- 98,333÷98,39	9) 2,592	/ 14,947 /	256	0.00000	82.59%	82.36%
49	0.80167	0.19833	0.04186	0.95814	95,767	97,264	82,119	15,145	274	0.00000	82.12%	81.78%
50	0.80868	0.19132	0.04431	0.95569	95,4 100,	.000 - 93,776 - 6	5,160 - 63	15,532	294	03 776 ÷ 100 00	1.44%	80.99%
:	:	:	:	:	:	· · · · · · · · · · · · · · · · · · ·		i/	: L	93,776 ÷ 100,00	:	:
3	:	:	:	:	:	99,937 - 9	0,111 - 9,759	0-67	:	:	:	:
:	:	:	:	:	:	:	:	:	:	:	:	:
109	0.99975	0.00025	0.96978	0.03022	16	16	0	16	18	0.00000	0.00%	0.00%
110	0.99977	0.00023	0.97280	0.02720	7	7	0	7	9	0.00000	0.00%	0.00%
									End-of-	Year Transition	30.11	29.61
									Midy	ear Adjustment	-0.50	
										Calculated WLE	29.61	29.61
									S-0	C-K Table Value	29.61	

Calculating the Probability of Being An Active Labor Force Participant – Initially Inactive State

[A]	[B]	[C]	[D]	[E]	[F]	[G]	[H]	[1]	[J]	[K]	[L]	[M]
	S-C-K Tr	ansition Proba	bilities									
	Females With An Associate's Degree			In	Initial values for contrastic achort						(0% + 29.688%) ÷ 2
					Initial values for synthetic conort.			0 ÷ 100,000		0		
		100,000 3	: 98,399 ÷ 98,461		\setminus					Check	\backslash	Average for Mid Veer
	Inactive to	Inactive to	Active to	Active to	L \	\	Alive &	Alive &		Difference	Probability of	Discounting &
Age	Inactive	Active	Inactive	Active		Alive	Active	Inactive	Dead	On Alive	Being Active	Transitions
30	0.70303	0.29697	0.06164	0.93836	98,461	100,000	0	100,000	0		> 0.00%	¥ 14.84%
31	0.71164	0.28836	0.05738	0.94262	98.399	99,937	29,678	70,259	a 63	0.00000	29.68%	, 38.94%
32	0.72864	0.27136	0.05540	0.94460	98,333	> 99,870	48,202	51,667	67	7 0.00000	148.20%	1 53.86%
33	0.74605	00.027	00 222 - 55 55	4628	98,262	99,798	59,510	7 40,288	/ 1/72	170.00000	59.51%	63.00%
34	0.75996	99,937	x 98,333 ÷ 98,39	4949	98,186	99,721	66,493 /	33,228 /	/ 77 /	0.00000	66.49%	68.77%
35	0.75831	(0 - 0 02020				99,628	71,051	28,587	83 /	/ 0.00000	71.05%	72.72%
36	0.76535	(0 X 0.93836	$+100,000 \times 0.25$	9697) X 98,3	99÷98,461	98,550	74,389	25,261 /	89/	0.00000	74.39%	75.50%
37	0.76975	0.23025	0.04837	0.95163	97,923	99,453	/16,617	2/2,837	96 /	0.00000	76.62%	77.35%
38	0.76201	(29,678 x 0.94	262 + 70,259 x 0	.28836) x 98	3,333 ÷ 98,399 ∤	99,348	78,086	/21,262	/105 /	0.00000	78.09%	78.71%
39	0.76977	0.23023	0.04585	0.95415	97,705	99,232	79,335	/ 19/897	/ 116/	0.00000	79.34%	79.76%
40	0.76561	(100.00	0 = 0 70202 + 0 -	. 0.06164)	08 200 - 08 461	99,104	80,175 /	1/8,929	/ 12/8	0.00000	80.17%	80.49%
41	0.75483	0 (100,00	$0 \times 0.70303 \pm 0.9$	(0.00104) X	98,399 ÷ 98,401	98,963	80,808	/18,155	/ 1/41	0.00000	80.81%	81.07%
42	0.75451	0.24549	0.04638	0.95362	97,288	98,808	81,329	/ 17,479 /	/155	0.00000 /	81.33%	81.52%
43	0.75211	(70,259 x 0.)	71164 + 29,678 x	0.05738) x	98,333 ÷ 98,399	98,639	81/708	/ 16,931/	/ 169	0.00000 /	81.71%	81.97%
44	0.75803	0.21177	0.0112	0.70010	,,,,,,	J 98,454	\$2,225 /	16,2/9	/ 185	0.00000	(29.688% + 4	(9.20%) ÷ 2
45	0.76781	0.23219	0.04227	0.95773	06 740	00 757	7/82,588	15,664	/ 202	0.00009	62.35%	aź.3770
46	0.76876	0.23124	0.04105	0.95895	100,000 x (1 - 98	8,399÷98,461)	82,549	18,483 /	220	0.0000¢	82.55%	82.54%
47	0.77808	0.22192	0.03999	0.96001	96.289	97.794	82/540	/15,255/	238	0.00000	82.54%	82.47%
48	0,79302	0.20698	0.04037	0.95963	99,937 x (1	- 98,333÷98,39	9) 2,408	15,130	256	0.00000	82.41%	82.19%
49	0.80167	0.19833	0.04186	0.95814	95,767	97,264	81,981	15,283	274	0.00000	81.98%	81.66%
50	0.80868	0.19132	0.04431	0.95569	100,0	00 - 29,678 - 70,	259 - 63	15,637	294	29 678 ÷ 100 0	1.33%	80.99%
	:	:	:	:	·			(7) /:	: L	29,070 . 100,0	:	:
3	:	:	:	:	: [99,937 - 48,20	02 - 51,007 - 0	6/ :	:	:	:	:
	:	:	:		:	:	:	:	:	:	:	:
109	0.99975	0.00025	0.96978	0.03022	16	16	0	16	18	0.00000	0.00%	0.00%
110	0.99977	0.00023	0.97280	0.02720	7	7	0	7	9	0.00000	0.00%	0.00%
									End-of-	Year Transition	27.09	27.09
									Midy	ear Adjustment		
									C	Calculated WLE	27.09	27.09
									S-0	-K Table Value	27.09	

Front and Uniform Loading Compared to Probability of Being an Active Labor Force Participant



rigure 4



Females With An Associate's Degree

30-Year Old Initially Active Females With an Associate's Degree



	I	loss for	Cumulative			
Loss Period]	Period	Loss			
Through Age 70:	\$	300,000	\$	300,000		
Age 70 On:	\$	30,000	\$	330,000		

Table 1 -Presentation of Losses with Assumed Part-Time EmploymentAfter Age 70

Endnotes

- ² In general, if "t" is the fractional part of the age of the individual in question, then the desired probability is written as $P_x = [t \cdot \tilde{A}_{x+1} + (1-t) \cdot A_x]/100,000$, where the initial cohort size is 100,000 for both starting integer ages. The numerator in the right-hand expression is derived by linear interpolation of the difference between \tilde{A}_{x+1} and A_x : the interpolated value equals $A_x + t \cdot (\tilde{A}_{x+1} A_x)$ which equals $[t \cdot \tilde{A}_{x+1} + (1-t) \cdot A_x]$.
- ³ Because the age-earnings profile is a linear spline, the slight bump in earnings after age 66 is preserved in this figure. A different method, say, fitting a quadratic through the midpoints, would remove this bump.
- ⁴ The overstatement noted here is separate from that identified by Skoog and Ciecka (2006). In their analysis, they only measured the bias of the two shortcut methods compared to explicit use of the probability of labor force activity for a constant annual loss. They did not consider any age-earnings effects or the effect of part-time employment later in life.
- ⁵ Note that the horizontal axis in Figure 5 shows the age of the 30-year-old woman, not her remaining years of labor force activity. This latter variable equals her age minus 30. Thus, age 54.5 equates to a remaining work life of 24.5 years with a corresponding probability of 3.5 percent.
- ⁶ Even though 110 is the terminal age of the Markov process, the S-C-K WLE tables extend only to age 75. While it is possible to extend the WLE calculations for starting ages beyond 75, the paucity of data at older ages makes the resulting WLE estimates less reliable
- ⁷ It is sometimes argued that the mortality risk of the non-injured plaintiff need not be explicitly accounted for because his/her remaining life expectancy is greater than the injured person's remaining WLE. This argument suffers from the same shortcomings as does front loading: it sets the non-injured plaintiff's probability of survival equal to one up to his or her remaining life expectancy and to zero thereafter, even though it is well know that the survival probability declines and remains positive for a period beyond the remaining life expectancy.
- ⁸ Use of the U.S. Census Bureau's PINC-04 tables for all persons with earnings may overcome this limitation.

¹ This is the table that the S-C-K WLE's are based upon. The values shown have been extended through age 110 according to the methodology presented in Arias (2010).